

$$\hat{d}(X_1) = \frac{\ln 2}{\ln(\hat{r}^k(X_1) / \hat{r}^{\lceil k/2 \rceil}(X_1))}$$